

# Oil Dispersion with a Turbine Mixer

A laboratory study was conducted to determine the factors influencing the dispersion of oil with a turbine mixer. Drop-size distributions as a function of time were related to the impeller diameter, power expended in relation to the liquid volume, and the final emulsion temperature.

It was surprising that higher temperatures produced smaller mean drop diameters but at the expense of a wider distribution. An optimal batch size for the emulsion was found to exist in processing. Below this size, tank surface and internal turbulence waste much of the energy; above this size, the energy per unit volume became a critical factor.

Other trials were made to determine the effect of the turbulence of the tank surface, tank geometry, number of impeller blades, and turbine configuration. These all significantly affect drop size and should be considered in the design and selection of dispersing equipment.

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## SCOPE

The emulsification of oil with a turbine mixer in a baffled cylindrical tank was correlated for the Sauter mean diameter as a function of time. Several time relationships are considered which describe the resulting mean drop diameter. The ultimate diameter that can be reached at infinite dispersion time is correlated to the operating conditions.

A size distribution computer program is described and applied to the measured emulsification data. Mean diameters in

the range of 1 to 30  $\mu\text{m}$  were evaluated. An analysis is made of the emulsion size distributions for the emulsions and the conditions which formed them.

Several different types and sizes of impellers were employed and these are evaluated on their ability to produce a desired size distribution rapidly. Different emulsion levels in the tank are related to the effective use of agitator power.

## CONCLUSIONS AND SIGNIFICANCE

Emulsification conditions and the time to produce a given Sauter mean diameter can be described by several relations. The simplest of these describes the mean diameter as a function of the power expended and time and is in the form:

$$d_{32} = \frac{0.02203 |V - 18.93|^{0.45}}{d_i^{4.41} N^{3.50} T^{0.573} t^{0.400}}$$

The confidence limits on  $d_i$  and  $N$  include the power number exponents  $\{d_i^5 N^3\}$  exponent as observed by Thornton and Buoyatiotis (1963). The equation is significant above the 99% level having an  $F$  test of 30.8. This equation applies in our system to a six-bladed flat turbine in a baffled tank.

It was observed that higher temperatures (lower viscosity and surface tensions) produced smaller drop diameters as indicated, but this was at the expense of wider distribution which is not shown by the equation.

A more accurate measure of change in particle size with time may be obtained by plotting the mean diameter against the reciprocal of time. This results in a straight line for times greater

than two hours for our system. The intercept ( $t = \infty$ ) is the smallest mean diameter that can be produced under these emulsifying conditions. When the difference between actual and ultimate diameter is plotted on semilog paper, a straight line results for all observations. This provides an accurate way to predict mean drop diameter with time when the ultimate diameter for particular operation is known. A correlation of the ultimate diameter and emulsification conditions has been determined.

An optimum batch size for emulsion production was determined to exist in the tank. This optimum occurred when the level in the tank was roughly equal to the tank diameter. Below this level, turbulence of the tank surface wasted much of the energy; above this level, the energy per unit volume decreased markedly.

Other trials were made to determine the effect of turbulence of the tank surface, the number of impeller blades, and turbine configuration. These all significantly affect drop size and should be considered in the design of dispersion equipment.

## BACKGROUND

In the production of large emulsion sizes in the range of 1,000  $\mu\text{m}$  and larger, the effect of coalescence is pronounced as described by Brodkey (1967). In contrast, Shinnar (1961) was able to control coalescence by surface active agents and showed that the Sauter mean diameter of an emulsion produced was proportional to the impeller speed to  $-3/4$  power. On the other hand, Sprow (1967) measured emulsion diameters near a turbine impeller in dilute iso-octane and salt water emulsion. These samples showed little

coalescence and gave an impeller speed exponent of  $-6/5$  power.

Mlynek and Resnick (1972) used water and a mixture of iso-octane and carbon tetrachloride in which there was no dependence of drop size on location in the vessel. They concluded that the mean emulsion diameter was correlated with the Weber number ( $N^2 d_i^3 \rho / \sigma$ ) to the  $-0.6$  power.

Droplet-size distributions in a baffled vessel were determined by Thornton and Buoyatiotis (1963). Drop-size distributions were given at zero holdup as a correlation containing power per unit

volume cubed in a dimensionless group to the  $-0.32$  power. The net result is an exponent on the power/volume term of  $-0.96$ .

We have been concerned with the production of emulsions with mean diameters of 1 to 10  $\mu\text{m}$ . In this size range, the emulsion behaves more nearly like solid particles with little coalescence. These emulsions are produced at high volume fractions of the dispersed phase at 38.9%. Although some of these authors cited investigated emulsions with low coalescence, few studies have been done at high-volume fractions.

In addition, there was also a particular interest in the drop-size distribution produced in these studies. Both Lapple (1963) and Keey and Glen (1969) reported diameter-frequency plots which show a logarithmic-normal distribution for drop size. The geometric deviation, which is the ratio of the particle sizes within a simple standard deviation, was observed to fall between 2 and 3. A narrow distribution will have a large geometric deviation.

Chang, Sheu, Tatterson and Dickey (1980) and Van 't Riet (1975) have shown that the breakup of an emulsion occurs near the impeller. All agitators shed vortices from the tips of the impeller blades under the turbulent flow conditions. In high-speed stereo films of the phenomena by Tatterson, the large drops of oil can be seen to stretch and break up in the vortex. This was the only place the breakup occurred. Except under extreme conditions, the flow regime at the tip of the impeller blades controls the vortex formation and, therefore, the rate of emulsification.

The impeller in any mixing application has two functions: pumping and turbulence. Gross turbulence is largely the result of the pumped fluids interacting with the baffles and walls. Localized turbulence is the result of the vortices shed by the impeller. Both functions require energy from the impeller. Fondy (1963) has shown the ultimate diameter of emulsion produced is controlled solely by tip speed of the impeller with a given emulsion at constant temperature. Most of the energy consumption, on the other hand, seems to go into moving (pumping) the fluid and in gross turbulence. However, for breakup of a drop in an emulsion, energy must be put into the drop to overcome surface and viscous forces. This is a difficult task and therefore emulsification is very energy-inefficient. Fondy recommends that the impeller diameter be reduced to minimize power consumption since the pumping action increases dramatically with the impeller diameter. Van't Riet (1975) has estimated that only 10% of the fluid pumped passes through the high shear region. Finally Rushton (1977) states that dimensionless groups generally used to describe mixing and fluid flow do not fully account for the interactions affecting emulsification.

## PROCEDURES

The emulsification work was performed on a specially designed test stand with a 0.75-hp (0.56-kW) variable speed mixer. This allowed the application of relatively large power input into the 35-L baffled glass tank. The mixer motor and impeller could be moved up and down on the stand with a counterbalance arrangement so that the impeller could be precisely located above the bottom of the tank. The tank itself was located in the center of a turntable mounted on roller bearings. The torque transmitted to the tank could be measured with a spring scale connected to a 231.8-mm torque arm from the turntable. The tank was strapped to a support on the turntable.

Four impellers were used: three flat blade turbines and a marine impeller. The flat blade turbines were 114.3 and 152.4 mm in diameter and 25 to 35 mm wide. The 152.4 mm (35 mm wide) turbine had six blades while one 114.3-mm turbine had six blades 25 mm wide and the other had 12 blades. The marine impeller was 114.3 mm in diameter.

The tank diameter was 285 mm and had four 25-mm baffles attached and extending to about 12 mm from the tank bottom. The ratio of baffle width to tank diameter therefore was about 11.5. Total tank height was 610 mm although the largest emulsion batch used was 26.5 L extending only 410 mm up the wall.

The water-base polymer solution of about 0.220 Pa-s viscosity

was poured into the tank, then the impeller was adjusted to about 90 mm off the bottom to prevent air entrainment during the addition of oil. The oil to be emulsified consisted of a mixture of about 60% aromatic hydrocarbon diluted with kerosene having a specific gravity of about 1.0. The oil viscosity was 0.008 to 0.010 Pa-s, and it was completely immiscible in the water solution. It was stored in a plastic tank from which it could be metered slowly through plastic tubing into the mixing tank to give 38.8% oil by weight (and volume) over a period of 10 to 20 minutes. The oil was added at such a location that it was immediately drawn into the turbine for initial dispersion. Once all of the oil was added, the turbine height was adjusted to one-third the distance from the tank bottom to the emulsion surface. Batch samples were taken from the rapid moving portion of the tank. It was found the mean drop sizes of the samples taken before 60 minutes were not stable. Consequently, the first recorded samples were taken 90 minutes after the start of oil addition. No coalescence was observed in the samples taken after 90 minutes. The samples were diluted and analyzed immediately on the Coulter counter. A data summary is given in Table 1. The data are for the turbine impellers except where marked as being for the marine impeller.

The temperature of the emulsion was measured as each sample was removed. Since most of the mixing energy ended up in emulsion, the temperature tended to rise. At higher impeller speeds, this became a problem. Therefore, a number of runs were made with the temperature of the tank controlled by a water jacket around the tank to account accurately for these variations.

## SIZE DISTRIBUTIONS

A computer program was written to take each of the volumetric particle-size distributions from the Coulter counter and convert it to surface-area-weighted distribution from which the Sauter mean diameter was obtained. The cumulative distribution from the Coulter counter was converted to a probability log-diameter function to describe the distribution. An example of the output from this program for Batch 9 at 300 minutes mixing time is given in Table 2. The converted diameter and its log for each of the fractions is shown (by surface area). These fractions are converted to probabilities measured as the number of standard deviations above or below the mean where they lie. Thus, 68.3% of the particles lie within one standard deviation of the mean; 95.5% lie within two sigma. When these data are correlated statistically, the intercept of the regression represents the log of median diameter. This diameter along with the Sauter mean are given. For a perfect fit of the data, these two diameters will be the same.

When the data are actually plotted on probability paper, Figure 1, it is evident that the data above the median and the data below the median form two distinct groups. This has been observed by other experimenters. Each half can be correlated in a similar manner giving two best lines. The slopes of both of these are given in addition to their intercept (median). For a perfect fit, again, these three lines would be the same. To compare them, a  $t$ -test is given for each of the lines. A  $t$ -value greater than 2.5 is significant at the

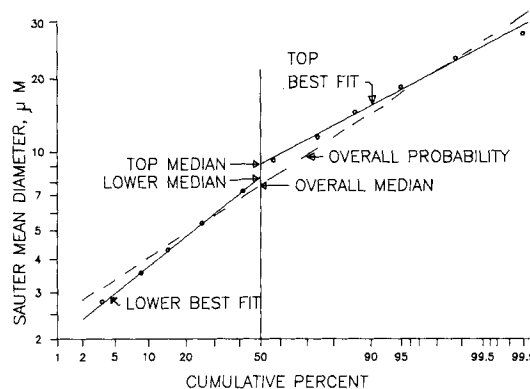


Figure 1. Typical probability curve, Run 9, 300 minutes.

TABLE 1. TURBINE MIXING TRIALS, DATA SUMMARY

Turbine Dia., mm	Batch Size L	Speed $s^{-1}$ (m/s)	Power W	Temp. $^{\circ}C$	Time min	$d_{32}$ $\mu m$	Slope Dstrb	Slope Bottom	Slope Top	Slope $d_{32}$ -T m-s	Time Const. s
Run 9 152.4	18.9	9.17	197 201 204 201	37.0 42.0 46.0 49.0	90.0 150.0 210.0 300.0 Ult.	18.79 13.66 10.88 8.13 3.05	0.3893 0.4530 0.4448 0.4873	0.6251 0.5615 0.6014 0.6132	0.2266 0.3128 0.3063 0.3954		
Run 10 152.4	Tip Speed Early Samples Unstable 11.4	(4.39) 7.5	67 67	36.0 36.0	300.0 330.0 Ult.	29.14 26.69 24.73	0.3819 0.4266	0.6010 0.6152	0.2463 0.2694	0.0956 0.0600	3,546 8,100
Run 11 152.4	11.4	10.83	162 162 162 162	40.0 43.0 46.0 46.0	90.0 150.0 210.0 300.0 Ult.	9.99 7.59 5.81 4.25 0.88	0.4363 0.4743 0.4863 0.4785	0.6045 0.5425 0.5588 0.5144	0.3536 0.4298 0.4763 0.4968	0.0610	4,560
Run 13 152.4	26.5	9.17	234 230 230 233	36.0 41.0 46.0 50.0	90.0 150.0 210.0 300.0 Ult.	17.13 15.77 13.82 9.16 4.75	0.3601 0.4110 0.4554 0.4501	0.5396 0.5458 0.5891 0.2379	0.2587 0.2980 0.3519 0.5361	0.0995	3,612
Run 14 152.4	Mixer Speed Surging 18.9	(4.39) 9.17	208 204 204 204	37.0 41.0 44.0 46.0	90.0 150.0 210.0 300.0 Ult.	12.43 10.26 9.03 7.24 3.91	0.5023 0.5513 0.5746 0.5464	0.5546 0.7053 0.6389 0.6893	0.3927 0.4466 0.5002 0.4804	0.0602	4,596
Run 15 152.4	11.4	9.17	130 130 122 122	35.0 40.0 42.0 43.0	90.0 150.0 210.0 300.0 Ult.	16.85 14.75 10.83 8.98 3.86	0.4267 0.4998 0.4406 0.4649	0.6468 0.6619 0.6542 0.5894	0.2663 0.3338 0.3703 0.3571	0.0934	3,636
Run 16 152.4	18.9	9.17	204 204 212 212	37.0 42.0 46.0 48.0	90.0 150.0 210.0 300.0 Ult.	10.36 8.27 7.59 5.46 3.06	0.4717 0.5205 0.4635 0.5201	0.6774 0.6610 0.5392 0.5918	0.3569 0.4269 0.4065 0.4822	0.0494	5,364
Run 17 152.4	First Samples Were Lost 26.5	7.5	128 125	38.0 40.0	210.0 300.0 Ult.	24.47 23.34 20.52	0.3378 0.3294	0.4509 0.4746	0.2652 0.2431	0.0502	9,012
Run 18 152.4	Lost Baffle At 225 Min. 18.9	10.83	298 298 298 298	40.0 50.0 56.0 56.0	90.0 150.0 210.0 300.0 Ult.	5.70 3.92 2.95 2.43 1.01	0.5431 0.5620 0.5354 0.5338	0.5904 0.6084 0.6375 0.6168	0.5523 0.5216 0.4891 0.4641	0.0254	9,966
Run 19 152.4	Rerun No. 12 18.9	7.50	110 110 110 110	34.0 36.0 36.0 36.0	90.0 150.0 210.0 300.0 Ult.	21.89 18.43 16.10 14.27 10.26	0.4649 0.4891 0.5288 0.4918	0.6694 0.6794 0.7566 0.4634	0.3375 0.3694 0.4042 0.4423	0.0733	4,080
Run 20 152.4	Alternate Turbine 18.9	9.17	216 216 216	40.0 49.0 51.0	90.0 210.0 300.0	9.28 5.41 3.72	0.5489 0.5689 0.5976	0.6190 0.5881 0.8185	0.4791 0.5769 0.5054	0.0695	
Run 21 152.4	Reduced Speed to Hold Temp. Constant 26.5	10.00	324 324 324 324	30.0 39.0 48.0 58.0	90.0 150.0 210.0 300.0 Ult.	10.44 8.87 7.30 5.77 2.76	0.4878 0.5381 0.5524 0.5502	0.6019 0.6451 0.6783 0.5881	0.3981 0.4748 0.4791 0.5373	0.0556	4,896
Run 25 152.4	With Floating Cover 18.9	9.17	197 208 208 208	38.0 44.0 48.0 49.0	90.0 150.0 210.0 300.0	5.26 6.54 5.39 4.31	0.4551 0.5101 0.5584 0.5199	0.2475 0.5402 0.5761 0.5804	0.6635 0.4731 0.5716 0.5150	0.0402	

TABLE I Continued

Turbine Dia., mm	Batch Size L	Speed s <sup>-1</sup> (m/s)	Power W	Temp. °C	Time min	d <sub>32</sub> μm	Slope Dstrb	Slope Bottom	Slope Top	Slope d <sub>32</sub> -T m-s	Time Const. s		
Run 33 152.4	Alternate Turbine 18.9	9.17	193 202 193 202	34.0 40.0 44.0 47.0	90.0 150.0 210.0 300.0	15.81 10.12 7.27 5.29	0.4516 0.4656 0.4880 0.5043	0.6461 0.5948 0.6367 0.7119	0.3391 0.3533 0.3782 0.3758	0.0870			
Run 22 114.3	18.9	12.22	148 154 154 159	36.0 40.0 44.0 46.0	90.0 150.0 210.0 300.0	13.57 11.01 8.88 7.76	0.4972 0.5512 0.5443 0.5510	0.6813 0.6247 0.6966 0.5484	0.3880 0.4841 0.4741 0.5352				
			(4.38)	Ult.	4.05							0.0630	4,434
Run 23 114.3			Marine Propeller 18.9	12.22	143 143 143 143	34.0 39.0 42.0 45.0	90.0 150.0 210.0 300.0	15.57 12.53 9.83 8.04	0.4766 0.4966 0.5512 0.5480			0.7374 0.5438 0.6948 0.6668	0.3098 0.3902 0.4500 0.4734
Run 24 114.3	Marine Propeller 18.9	12.22	148 154 154 148	36.0 40.0 44.0 46.0	90.0 150.0 210.0 300.0	18.17 15.94 13.36 10.53	0.4556 0.4709 0.4770 0.6022	0.6042 0.4853 0.5413 0.7306	0.3897 0.4029 0.4101 0.5204	0.0852	3,840		
		(4.38)	Ult.	6.29									
Run 27 114.3	26.5	12.22	148 158 158 158	33.0 36.0 38.0 40.0	90.0 150.0 210.0 300.0	26.56 23.99 21.12 17.79	0.3157 0.3190 0.3345 0.3266	0.4589 0.4834 0.4379 0.5653	0.2240 0.2436 0.2171 0.2291				
			(4.38)	Ult.	12.41								0.1044
Run 28 114.3			18.9	14.45	263 263 263 269	43.0 46.0 52.0 54.0	90.0 150.0 210.0 300.0	5.58 4.20 3.43 3.52	0.4587 0.4386 0.4922 0.3655	0.5423 0.5642 0.5258 0.2498	0.3748 0.3941 0.5110 0.4459		
					(5.19)	Ult.	1.65						0.0252
Run 31 114.3	18.9	14.45			216 228 228 228	38.0 42.0 47.0 51.0	90.0 150.0 210.0 300.0	16.71 10.20 7.36 5.03	0.3627 0.4214 0.4504 0.4499	0.5419 0.6235 0.5305 0.6268	0.2574 0.3541 0.4225 0.3518		
					(5.19)	Ult.	0.15						0.0912
Run 32 114.3			High Torque Fluctuations 11.4	12.21	91 87 87 87	30.0 33.0 33.0 35.0	90.0 150.0 210.0 300.0	19.27 13.99 11.85 9.51	0.4393 0.4440 0.4258 0.4261	0.5973 0.6435 0.5810 0.6004	0.3167 0.2828 0.3009 0.3472		
			(4.39)	Ult.	6.17							0.0684	426
Run 35 114.3	Repeat 31 With Cooling Jacket 18.9	14.45	246 251 246 251	30.0 33.0 36.0 35.0	90.0 150.0 210.0 300.0	12.72 9.85 7.86 6.33	0.3848 0.4272 0.4066 0.4370	0.6164 0.5135 0.6188 0.6128	0.2688 0.3121 0.3046 0.3486	0.0546	4,944		
	(5.19)	Ult.	3.54										
Run 36 114.3	Repeat 22 With Cooling Jacket 18.9	12.21	158 158 163 163	24.0 25.0 26.0 26.0	90.0 150.0 210.0 300.0	17.23 14.75 13.49 12.38	0.3116 0.3769 0.5385 0.3596	0.5094 0.5780 0.2319 0.4650	0.2004 0.2434 0.2319 0.2337				
	(4.39)	Ult.	10.39									0.0384	6,432
Run 38 114.3	With Floating Cover 18.9	14.45	251 270 251 257	31.0 33.0 34.0 34.0	90.0 150.0 210.0 300.0	8.20 5.86 4.74 4.11	0.4423 0.4653 0.4658 0.4814	0.4506 0.5284 0.6508 0.5802	0.3300 0.3459 0.3643 0.3985	0.0330			
Run 40 114.3	Repeat 35 With Cooling 18.9	12.21	158 158 163 163	35.0 40.0 43.0 45.0	90.0 150.0 210.0 300.0	13.11 11.26 9.60 8.27	0.4769 0.4420 0.4575 0.4464	0.6178 0.5220 0.6204 0.4406	0.3301 0.3407 0.3364 0.3972				
Run 41 114.3	12 Blade Impeller 18.9	12.21	218	35.0	90.0	9.15	0.4932	0.6884	0.3608			...	

TABLE I Continued

Turbine Dia., mm	Batch Size L	Speed s <sup>-1</sup> (m/s)	Power W	Temp. °C	Time min	d <sub>32</sub> μm	Slope Dstrb	Slope Bottom	Slope Top	Slope d <sub>32</sub> -T m-s	Time Const. s
			218	42.0	150.0	7.34	0.4750	0.6054	0.3763		
			218	45.0	210.0	6.32	0.5130	0.5423	0.4063		
			218	48.0	300.0	5.12	0.5278	0.6736	0.4325		
										0.0348	
Run 42 114.3	12 Blade, High Temp. 18.9	14.45	351	44.0	90.0	4.80	0.5293	0.7097	0.4162		
			351	53.0	150.0	3.63	0.5392	0.6450	0.4743		
			351	58.0	210.0	3.00	0.5421	0.6169	0.5128		
			351	61.0	300.0	2.56	0.6271	0.6614	0.5589		
										0.0180	
Run 43 114.3	12 Blade, Reduced Speed 18.9	10.0	125	28.0	90.0	29.19	0.3460	0.4518	0.2227		
			125	33.0	150.0	21.80	0.4319	0.6272	0.2633		
			122	36.0	210.0	18.91	0.4183	0.6104	0.2702		
			125	39.0	300.0	15.58	0.4449	0.6444	0.3183		
										0.1326	
Run 44 114.3	12 Blade, With Cooling 18.9	14.45	357	38.0	90.0	4.87	0.5000	0.6878	0.3904		
			357	39.0	150.0	3.94	0.4694	0.5498	0.3777		
			357	45.0	210.0	3.30	0.4634	0.5820	0.3846		
			357	50.0	300.0	2.69	0.4434	0.5963	0.3948		
										0.0270	
Run 45 114.3	12 Blade, With Cooling 18.9	12.22	257	38.0	90.0	8.93	0.4977	0.6434	0.3949		
			218	43.0	150.0	7.22	0.4834	0.5958	0.4201		
			222	46.0	210.0	6.23	0.5029	0.6089	0.4567		
			218	49.0	300.0	4.82	0.5457	0.7037	0.4687		
										0.0516	
Run 46 114.3	Alternate Blades Trimmed 18.9	12.22	158	31.0	90.0	10.90	0.6016	0.6111	0.7071		
			158	36.0	150.0	8.34	0.4741	0.5082	0.3759		
			158	39.0	210.0	6.31	0.5040	0.5528	0.3681		
			163	41.0	300.0	5.30	0.5003	0.6335	0.3867		
										0.0630	
Run 48 114.3	Alternate Blades Trimmed 18.9	14.45	269	40.0	90.0	5.35	0.4541	0.6615	0.3289		
			275	45.0	150.0	3.82	0.4743	0.5891	0.4056		
			275	49.0	210.0	3.07	0.4777	0.5984	0.4277		
			275	52.0	300.0	2.46	0.5118	0.5727	0.5101		
										0.0330	
Run 49 114.3	Alternate Blades Trimmed 18.9	12.22	158	32.0	90.0	15.67	0.4385	0.6119	0.2977		
			158	36.0	150.0	10.69	0.4453	0.6667	0.3706		
			158	39.0	210.0	8.39	0.4673	0.5195	0.3630		
			158	42.0	300.0	6.91	0.4592	0.5741	0.3979		
										0.0828	

98% level. All data were correlated much better when treated in two segments, and the bottom of the curve invariably produced a larger *t*-test (Table 2) as shown in the example. Inspecting the summary of the data in Table 1 shows that the overall slope of the distribution generally became larger (wider distribution) as agitation time increased. On further inspection, the distribution or slope of the top half of the emulsion increased considerably as emulsification continued. Since the median diameter is different for each of these, what appears to be happening is that the more narrow distribution of the larger particles is being preferentially broken down into the smaller ones. The smaller particles already present are changed very little. This process will continue until an ultimate particle diameter is reached.

#### EMULSIFICATION TIME

If the Sauter mean diameter is plotted against the reciprocal of the time, a nearly straight line is achieved after about 120 minutes of agitation. Extrapolating this line to infinite time (the intercept) gives that ultimate diameter. This was demonstrated by Fondy and Bates (1963). The data for Batch 9 are plotted this way in Figure 2. If the ultimate diameter subtracted from the mean diameter is

TABLE 2. SAMPLE OF EMULSION ANALYSIS  
Batch 9, 300 min, Batch Size—18.91, Speed—9.17 rps, 150-mm  
diameter flat-blade turbine  
Tip Speed = 4.39 m/s  
0.269 measured hp input, power/volume—10.60 W/L  
Emulsion Distribution Analysis

Mean Diameter	Log Dia.	Area-Weighted Fraction	Prob. Function
28.5096	3.3502	0.0011	3.0568
22.6513	3.1202	0.0115	3.2699
17.9778	2.8891	0.0509	1.6371
14.2548	2.6571	0.1313	1.1222
11.3144	2.4261	0.2807	0.5794
8.9800	2.1950	0.4536	0.1172
7.1274	1.9639	0.3914	-0.2740
5.6572	1.7329	0.2520	-0.6674
4.4900	1.5019	0.1506	-1.0352
3.5609	1.2700	0.0799	-1.4075
2.8264	1.0390	0.0368	-1.7895
Sauter Mean Diameter: 8.13.		Median Diameter: 7.65.	
		68% of Particles Fall between 4.70 and 12.46 μm.	
		95% of Particles Fall between 2.94 and 19.89 μm.	
Slope of Probability Curve:		T Test: 25.51	
		0.4873	
Slope of Bottom Half: 0.6132		Median: 8.47 T = 46,170.40	
Slope of Top Half: 0.3954		Median: 8.97 T = 580.63	

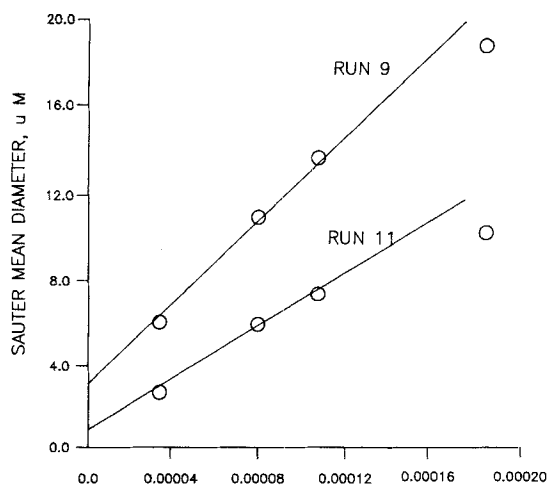


Figure 2. Extrapolation of emulsion size as a reciprocal of time.

plotted on semilog paper against time, the result is a very good fit even at the earliest times, Figure 3. This shows that the ultimate diameter is exponentially approached and the slope of this curve is the reciprocal of the time constant. This has been calculated for all of the data, Table 1. The value of the intercept was calculated for each time beyond 90 minutes from the graphically determined slope. These intercepts were then averaged to give the value in the table. Ideally an iterative procedure on the ultimate diameter would give a better fit of the data but this is not practical within the range of measurement errors encountered. Thus only one iteration is used. Table 1 shows that time constants of 50 to about 150 minutes are observed in our system. This means that 63.2% of the remaining change is observed during the period of one time constant.

It is instructive to correlate the ultimate diameter to the independent variables that were measured. This results in the following correlation with a *F*-test of 64:

$$d_u = \frac{1.214 \times 10^{15}}{U^{6.84} T^{1.73}}$$

This correlation gives a stronger response of turbine tip speed (*U*) on the ultimate diameter than observed by Fondy and Bates for a *fixed time* observation.

It was also found that the ultimate diameter was related inversely to the emulsification temperature to the 1.7 power. The temperature was included as a way to compensate for small temperature changes and not to define property changes resulting from the temperature level. Because of the relation of power and speed, the change in temperature will affect the power because of viscosity and surface tension changes at the same tip speed. Therefore, different exponents can be expected on the temperature when correlated with tip speed as opposed to a correlation with power consumed.

The rate with which the distribution approaches the ultimate diameter has been determined from the slope of the curve for the mean diameter vs. the reciprocal of time as well as the time constant. This slope is given in the next to the last column of Table 1 and can be considered as an inverse function of the time constant. Correlations of both were attempted with the slope giving the best correlation. The slopes were correlated at the 95% level (*F* = 7.4) by the equation:

$$\text{Slope} = \frac{3.517 T^{0.568} U^{0.557}}{p^{0.761}}$$

Since Power is proportional to the cube of the tip speed:

$$\text{Slope} = f\left(\frac{U^{0.557}}{(U)^{3(0.761)}}\right) = f(U^{-1.726})$$

This shows that a faster change (higher slope) is obtained with higher temperatures and liquid volumes but slower change results from high power levels. For the rate of approach to the ultimate

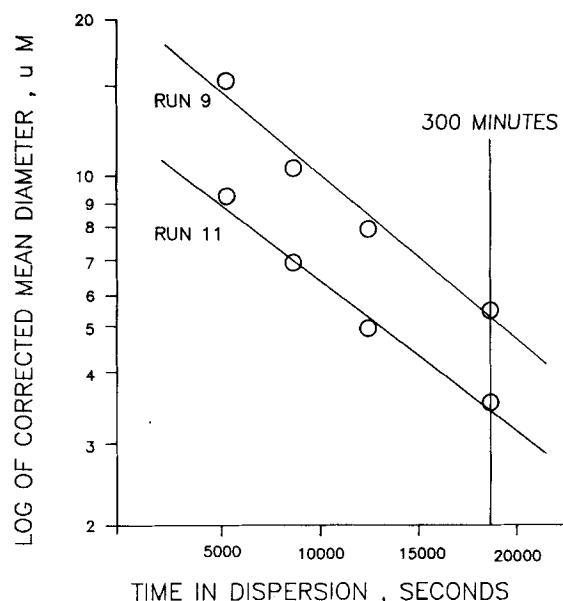


Figure 3. Change in the log of corrected diameter with time.

diameter, Fondy and Bates observed that the mean diameter varied with tip speed to the  $-1.8$  power. Our overall correlation of mean diameter at a fixed time shows an exponent of  $(-1.73)$  as can be noted in the equation for the slope given above.

It has been noted that the ultimate diameter is primarily controlled by the tip speed (and temperature). Changes in other parameters such as turbine shape, volume in tank, and fluid properties have only a minor effect. They do, however, determine how quickly this ultimate diameter is reached. Therefore, the effects of these other parameters should be understood.

#### VOLUME EFFECTS

The diameters obtained after 300 minutes of dispersion have been plotted for the 150-mm-diameter impeller in Figure 4. It shows that the Sauter diameter reaches a minimum for all speeds at about 19 L in the tank. The same shaped curves are produced by the ultimate diameter as a function of volume except for the highest speed at the lowest volume, where the diameter differences

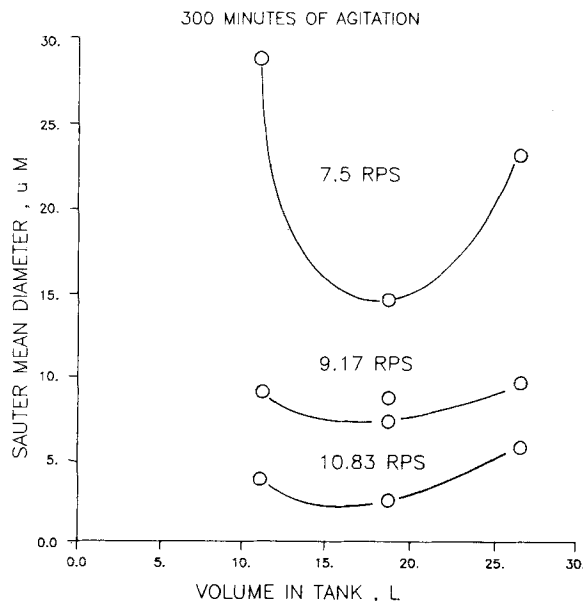


Figure 4. Effect of tank level on emulsion size.

are as large as the scatter. This minimum corresponds to a level of about 295 mm of emulsion in the tank. Since the tank is 285 mm in diameter, this corresponds to roughly a height equal to the diameter. The data show that high liquid volumes produce lower energy input per unit volume. It appears that above the optimum liquid volume, power remains constant while with more liquid the power is spread over a greater volume. At lower liquid levels, total energy consumption decreases as gross turbulence and surface activity appear. Although the power per unit volume seems to remain the same (at constant tip speed), much of the energy is wasted on turbulence. The emulsification comes primarily from the vortices shed from the turbine tip, not in gross turbulence.

## OTHER VARIABLES

A floating cover was added to the tank to prevent surface activity and air entrainment into the vortex systems. Runs 25 and 38 were made under these conditions. A comparison between these and Runs 16 and 35 show that the total power dissipation was not significantly changed but that the mean drop size was markedly decreased.

In Runs 23 and 24, a marine type impeller was used in place of same size flat turbine (Run 22). The vortex shedding from the marine impeller is completely different from that of a turbine. Because of the large pumping action of the marine impeller, the vortices probably receive less power input than those of the flat blade turbine. They tend to be a continuous trailing flow pattern below the propeller, and, as a result, are more coherent and less effective in emulsion production. Examination and comparison with the equivalent Run 22 for the turbine show no practical change in mean drop diameter and a very small reduction in power consumption. Because of the large amount of gross turbulence produced by the marine impeller, it is not an attractive substitute for the flat-bladed turbine.

The number of vortices formed by an impeller is in proportion to the number of blades on the impeller. Our basic turbine contained six blades which is typical of a flat turbine. A second turbine having 12 blades was fabricated and used in the last nine runs (41–49). As expected, the 12-blade impeller allowed us to put more power into the emulsion at the same tip speed. This resulted in substantially smaller mean particle diameters. For the 12-bladed impeller, the blade shape was changed slightly by machining 8 mm from the top or bottom of alternate blades. This produced as many vortices, but would not have the same amount of pumping action and gross turbulence. Comparing Runs 46–49 with Runs 22 and 28 show that the power consumption is reduced at the same speed but that the mean drop diameter remains about the same. Thus, turbine design can be an important factor in effective emulsification. The increasing number of blades has a practical limit when the vortex from one blade tip interferes with the vortex from another tip. For this reason, the staggered blades are an attractive way to solve this problem.

## NOTATION

$A$	= particle surface area, $m^2$
$d_I$	= impeller diameter, $m$
$d_u$	= ultimate diameter (Sauter mean), $\mu m$
$d_{32}$	= Sauter Mean diameter, $\mu m$
$N$	= impeller speed, $rps$
$P$	= power dissipated by impeller, $N \cdot m/s = W$
$t$	= time, $s$
$T$	= temperature, $^{\circ}C$ .
$U$	= tip speed, $m/s$
$V$	= volume in vessel, $L$
$\sigma$	= interfacial tension, $N/m$
$\mu$	= viscosity, $N \cdot s/m^2$

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